

Quantitative Method

Assignment 7

Due December 5, 2006

1. Suppose that X has an exponential distribution,

$$f(x) = \theta \exp\{-\theta x\}, \quad x \geq 0$$

- (a) Find the mean, variance, skewness, and kurtosis of x .
- (b) What is the probability distribution of the random variable $y = e^{-x}$? What is $E[y]$? Prove that the distribution of this y is a special case of the beta distribution.

2. Given the following joint probability distribution

		X		
		0	1	2
Y	0	0.05	0.1	0.03
	1	0.21	0.11	0.19
	2	0.08	0.15	0.08

- (a) Compute the following probabilities:
 $\text{Prob}(Y < 2)$ $\text{Prob}(Y < 2, X > 0)$ $\text{Prob}(Y = 1, X = 1)$
- (b) Find the marginal distributions of X and Y
- (c) Calculate $E[x]$, $E[Y]$, $\text{Var}[Y]$, $\text{Cov}[X, Y]$, and $E[X^2Y^3]$.
- (d) Calculate $\text{Cov}[Y, X^2]$.
- (e) What is the conditional distribution of Y given $X=2$? What is the conditional distribution of X given $Y > 0$?
- (f) Find $E[Y|X]$ and $\text{Var}[Y|X]$. Obtain the two parts of the variance decomposition

$$\text{Var}[Y] = E_x[\text{Var}_y[Y|X]] + \text{Var}_x[E_y[Y|X]].$$

3. Text problem C.1 at page 738 (Wooldridge).

4. Text problem C.7 at page 740 (Wooldridge).